

Algebra Unit 4 Review

Brain Dump: List the first 15 perfect squares:

$$1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225$$

Multiplying Radicals - RULE

1. Multiply the outside together.
2. Multiply the inside together.
3. Simplify the radical.

Adding/Subtracting Radicals - RULE

1. Simplify all radicals
2. Then add/subtract the Like radicals

Simplify Practice: Answer the following.

a. $\sqrt{25}$

5

b. $\sqrt{49}$

7

c. $\sqrt{100}$

10

d. $\sqrt{18}$

$\sqrt{9 \cdot 2}$

$3\sqrt{2}$

e. $\sqrt{63}$

$\sqrt{9 \cdot 7}$

$3\sqrt{7}$

f. $5\sqrt{12x^6y^5z^4}$

~~$5(\sqrt{4 \cdot 3} \cdot \cancel{x} \cdot \cancel{y} \cdot \cancel{y} \cdot \cancel{y})$~~

$10x^3y^2z^2\sqrt{3y}$

g. $\sqrt{48}$

~~$\sqrt{16 \cdot 3}$~~

$4\sqrt{3}$

h. $\sqrt{24x^2y^8}$

~~$\sqrt{4 \cdot 6 \cdot x \cdot y \cdot y \cdot y \cdot y \cdot y \cdot y}$~~

$2xy^4\sqrt{6}$

i. $\sqrt{14}$

$\sqrt{14}$

j. $3\sqrt{96w^2x^2}$

~~$3\sqrt{16 \cdot 6 \cdot w \cdot w \cdot x \cdot x}$~~

$12wx\sqrt{6}$

k. $4\sqrt{20}$

~~$4\sqrt{4 \cdot 5}$~~

$8\sqrt{5}$

l. $6\sqrt{120xy^3}$

~~$6\sqrt{4 \cdot 30x \cdot y \cdot y \cdot y}$~~

~~$12y\sqrt{30xy}$~~

m. $2\sqrt{36}$

~~2 \cdot 6~~

12

Multiply Practice: Multiply the following radicals. Make sure they are in simplest form.

a. $\sqrt{2} \cdot \sqrt{18}$

$\sqrt{36}$

6

b. $\sqrt{5} \cdot \sqrt{10}$

$\sqrt{50}$

$\sqrt{25 \cdot 2}$

$5\sqrt{2}$

c. $\sqrt{8} \cdot \sqrt{32}$

$\sqrt{256}$

16

d. $\sqrt{2y^3} \cdot \sqrt{8y^3}$

~~$\sqrt{16y^6}$~~

$4y^3$

e. $\sqrt{18a^2} \cdot 4\sqrt{3a^3}$

~~$4\sqrt{54a^5}$~~

~~$4\sqrt{9 \cdot 6aaaa}$~~

$12a^2\sqrt{6a}$

f. $3\sqrt{4m^2} \cdot -2\sqrt{10m^8}$

~~$-6\sqrt{40m^{10}}$~~

~~$-6\sqrt{4 \cdot 10 m^{10}}$~~

$-12m^5\sqrt{10}$

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Add/Subtract Practice: Add or Subtract the following radicals. Make sure they are in simplest form.

a. $2\sqrt{5} + 6\sqrt{5}$

~~$8\sqrt{5}$~~
 $8\sqrt{5}$

b. $3\sqrt{7} + 2\sqrt{7}$

$5\sqrt{7}$

c. $4\sqrt{15} - 6\sqrt{15}$

$-2\sqrt{15}$

d. $6\sqrt{7} + 8\sqrt{10} - 3\sqrt{7}$

$3\sqrt{7} + 8\sqrt{10}$

e. $11\sqrt{5} - 2\sqrt{20}$

$-2\sqrt{4 \cdot 5}$

$11\sqrt{5} - 4\sqrt{5}$

$7\sqrt{5}$

f. $3\sqrt{3} + 6\sqrt{27}$

$6\sqrt{9 \cdot 3}$

$3\sqrt{3} + 18\sqrt{3}$

$21\sqrt{3}$

g. $3\sqrt{5} + 2\sqrt{500}$

$3\sqrt{5} + 2\sqrt{100 \cdot 5}$

$3\sqrt{5} + 20\sqrt{5}$

$23\sqrt{5}$

h. $3\sqrt{3} - 2\sqrt{12}$

$-2\sqrt{4 \cdot 3}$

$3\sqrt{3} - 4\sqrt{3}$

$-1\sqrt{3}$

i. $12\sqrt{50} + 6\sqrt{2}$

$12\sqrt{25 \cdot 2}$

$60\sqrt{2} + 6\sqrt{2}$

$66\sqrt{2}$

Putting It All Together: Put together everything you have learned about radicals.

a. $\sqrt{12}(\sqrt{9} - \sqrt{4})$

$\sqrt{12}(3 - 2)$

$\sqrt{12}(1)$

$\sqrt{12}$

b. $\sqrt{3}(\sqrt{3} + 2\sqrt{5})$

$\sqrt{9} + 2\sqrt{15}$

$3 + 2\sqrt{15}$

c. $\sqrt{5}(\sqrt{10} - \sqrt{15})$

$\sqrt{50} - \sqrt{75}$

$\sqrt{25 \cdot 2} - \sqrt{25 \cdot 3}$

$5\sqrt{2} - 5\sqrt{3}$

d. $-\sqrt{5}(\sqrt{10} + 3)$

$-\sqrt{50} - 3\sqrt{5}$

$-\sqrt{25 \cdot 2}$

$-5\sqrt{2} - 3\sqrt{5}$

e. $5\sqrt{6}(\sqrt{6} + 4\sqrt{5})$

$5\sqrt{36} + 20\sqrt{30}$

$5 \cdot 6$

$30 + 20\sqrt{30}$

f. $-3\sqrt{3}(4\sqrt{6} - 2\sqrt{2})$

$-12\sqrt{18} + 6\sqrt{6}$

$-12\sqrt{9 \cdot 2}$

$-36\sqrt{2} + 6\sqrt{6}$

Algebra Unit 4 Review

Rational vs Irrational: Classify each number as rational or irrational and explain why.

a. $\sqrt{15}$

I

b. $\frac{1}{4}$

R

c. $\sqrt{2} \cdot \sqrt{18}$

$\sqrt{36}$
R

d. $\sqrt{25} + \sqrt{1} = 6$

R

e. $\sqrt{7} + \sqrt{28}$
 $\sqrt{4.7}$
 $\sqrt{7} + 2\sqrt{7}$

$3\sqrt{7}$
I

f. $\pi + (-\pi) = 0$

R

g. $\sqrt{6}(2+5)$

$8 - 7\sqrt{6}$

I

h. $\sqrt{2}(\sqrt{18} + \sqrt{8})$

$\sqrt{36} + \sqrt{16}$
 $6+4$
 10
R

i. $4(\sqrt{9} + \sqrt{2})$

$4\sqrt{9} + 4\sqrt{2}$
 $12 + 4\sqrt{2}$
I

Critical Thinking:

Let the following variables represent a certain type of number:

A = 5

B = -5

C = $\sqrt{9}$

D = $\sqrt{6}$

E = $\sqrt{6}$

F = $\sqrt{25}$

Determine if the following sums or products will result in a rational or irrational number.

a. A + B

$5 + -5 = 0$

R

b. A + C

$5 + \sqrt{9}$

$5 + 3$

8
R

c. C + D

$\sqrt{9} + \sqrt{6}$

$3 + \sqrt{6}$

I

d. C + F

$\sqrt{9} + \sqrt{25}$

$3 + 5$

8
R

e. A x B

$5 \cdot -5$

-25

R

f. B x C

$-5\sqrt{9}$

-15

R

g. C x D

$\sqrt{9} \cdot \sqrt{6}$

$3\sqrt{6}$

I

h. C x C

$\sqrt{9} \cdot \sqrt{9}$

9

R

i. D + E

$\sqrt{6} + \sqrt{6}$

$2\sqrt{6}$

I

j. D x E

$\sqrt{6} \cdot \sqrt{6}$

6

R

k. E + F

$\sqrt{6} + \sqrt{25}$

$\sqrt{6} + 5$

I

l. B + F

$-5 + \sqrt{25}$

$-5 + 5$

0
R

Algebra Unit 4 Review

Polynomial Operations: Simplify the following completely.

a. $(4x + 3x^2 - 7) + (-6x^2 + 4)$

$$-3x^2 + 4x - 3$$

b. $(4x^2 - 3x - 2) - (9x^2 + 3x - 7)$

$$4x^2 - 3x - 2 - 9x^2 - 3x + 7$$

$$-5x^2 - 6x + 5$$

c. $(5x - x^2) + (-2x^2 + 2x - 9)$

$$-3x^2 + 7x - 9$$

d. $(-4x - 2x^2 - 6) - (-2x^2 + 8x - 6)$

$$-4x - \cancel{2x^2} - 6 + \cancel{-2x^2} + 8x + 6$$

$$-12x$$

e. $5x(3x + 7)$

$$15x^2 + 35x$$

f. $(x + 4)(x - 9)$

$$x^2 - 5x - 36$$

g. $(2x + 3)(-3x - 4)$

$$\begin{array}{r} \frac{-3x - 4}{2x} \\ \hline \frac{-6x^2 - 8x}{-9x - 12} \\ \hline -6x^2 - 17x - 12 \end{array}$$

h. $(-5x + 9)(-2x - 9)$

$$\begin{array}{r} \frac{-2x - 9}{-5x} \\ \hline \frac{10x^2 + 45x}{-18x - 81} \\ \hline 10x^2 + 27x - 81 \end{array}$$

i. $(x + 1)(x + 8)(x - 6)$

$$\begin{array}{r} \frac{x + 8}{x} \\ \hline \frac{x^2 + 8x}{1x + 8} \\ \hline x^3 + 9x^2 + 8x \\ \hline -x^3 - 8x^2 - 48x \\ \hline x^3 + 3x^2 - 46x - 48 \end{array}$$

j. $(x - 4)(x + 4)(x - 5)$

$$\begin{array}{r} \frac{(x^2 - 16)(x - 5)}{x^2} \\ \hline \frac{x^3 - 5x^2}{-16x - 80} \\ \hline x^3 - 5x^2 - 16x + 80 \end{array}$$

k. $(x - 5)^2$

$$\begin{array}{r} \frac{x - 5}{x} \\ \hline \frac{x^2 - 5x}{-5x + 25} \\ \hline x^2 - 10x + 25 \end{array}$$

l. $(x + 7)^3$

$$(x^2 + 14x + 49)(x + 7)$$

$$\begin{array}{r} \frac{x^2 + 14x + 49}{x} \\ \hline \frac{x^3 + 14x^2 + 49x}{7x^2 + 98x + 343} \\ \hline x^3 + 21x^2 + 147x + 343 \end{array}$$